Closure under morphisms  Given a finite alphabet $\Sigma$, a function $f : \Sigma^* \rightarrow \Sigma^*$ is a morphism if $f(\Sigma) \subseteq \Sigma$ and for all $a = a_1 \cdots a_n \in \Sigma^*$, $f(a) = f(a_1) \cdots f(a_n)$ ($f$ is uniquely determined by the value it takes on $\Sigma$).

Show that $\mathbb{P} = \mathbb{NP}$ if and only if $\mathbb{P}$ is closed under morphism.