

Refinements and Abstractions of Signal-Event (Timed) Languages

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Joint work with Béatrice Bérard and Antoine Petit

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Outline

1 Introduction

Signal-Event (Timed) Words and Automata

Signal-Event (Timed) Substitutions

Closure under substitutions

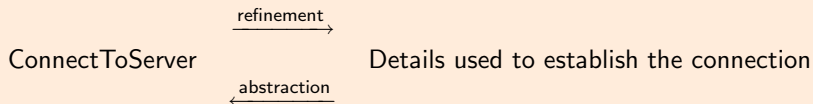
Closure under inverse substitutions

Conclusion

Refinements and Abstractions

Abstract level

Concrete level



Formalisation of refinement

Let $\sigma : A \rightarrow \mathcal{P}(B^*)$ be a substitution.

Abstract level

Concrete level

Action $a \in A$

$\xrightarrow{\text{refinement}}$ $\sigma(a) \subseteq B^*$

Behavior $w = abaac \in A^*$

$\xrightarrow{\text{refinement}}$ $\sigma(w) = \sigma(a)\sigma(b)\sigma(a)\sigma(a)\sigma(c) \subseteq B^*$

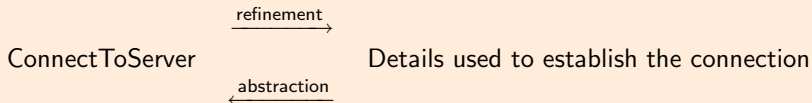
Language $K \subseteq A^*$

$\xrightarrow{\text{refinement}}$ $\sigma(K) = \bigcup_{w \in K} \sigma(w) \subseteq B^*$

Refinements and Abstractions

Abstract level

Concrete level

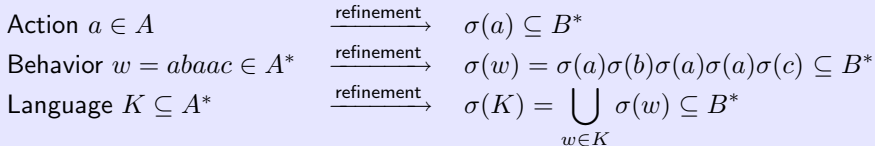


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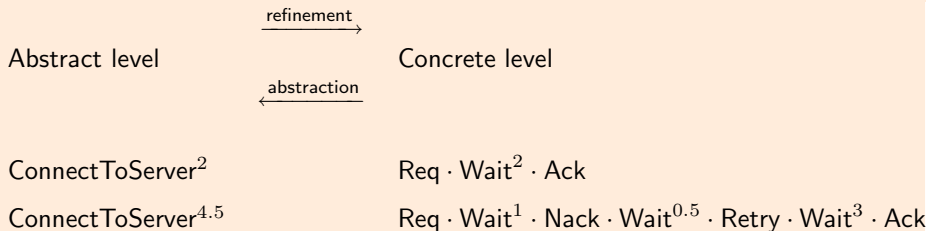
Abstract level

Concrete level



Adding time to the picture

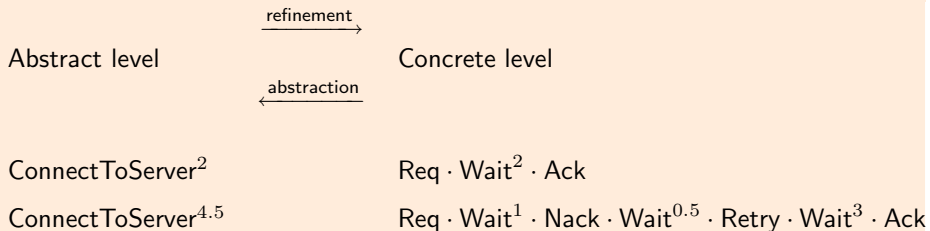
Timed refinement



An abstract action a with duration d should be replaced by a concrete execution (word) w with the same duration $\|w\| = d$.

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Signal-Event (Timed) Words

Asarin - Caspi - Maler 2002

- ▶ Σ_e finite set of (instantaneous) events
- ▶ Σ_s finite set of signals
- ▶ \mathbb{T} time domain, $\overline{\mathbb{T}} = \mathbb{T} \cup \{\infty\}$
- ▶ $\Sigma = \Sigma_e \cup (\Sigma_s \times \mathbb{T})$
- ▶ Notation: a^d for $(a, d) \in \Sigma_s \times \overline{\mathbb{T}}$
- ▶ Σ^∞ set of **signal-event (timed) words**
Example: $a^3 f f g b^{1.5} a^2 f$
- ▶ Signal stuttering: $a^2 a^3 \approx a^5$, $a^\infty = a^2 a^2 a^2 \dots$

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Signal-Event (Timed) Words

Unobservable signal τ

- ▶ Useful to hide signals:

Signal-event word $\xrightarrow{\text{hiding signals}}$ Classical timed words

$$a^3fb^1gfa^2f$$

$$\tau^3f\tau^1gf\tau^2f = (f, 3)(g, 4)(f, 4)(f, 6)$$

- ▶ $\tau^0 \approx \varepsilon$: an hidden signal with zero duration is not observable.
 $a^0 \not\approx \varepsilon$: a signal, even of zero duration, is observable.
 $\tau^2 \not\approx \varepsilon$: we still observe a time delay but the actual signal has been hidden.
Example : $a^2\tau^0a^1f\tau^0g\tau^1fb^2b^2b^2 \dots \approx a^3fg\tau^1fb^\infty$
- ▶ Signal-event words $SE(\Sigma) = \Sigma^\infty / \approx$

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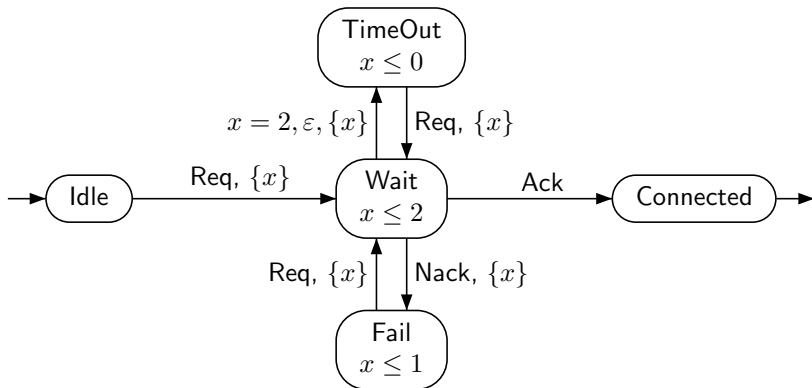
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Signal-Event (Timed) automata

- ▶ States emit signals
- ▶ Transitions emit (instantaneous) events



- ▶ Run : $\text{Idle}^3 \cdot \text{Req} \cdot \text{Wait}^2 \cdot \text{TimeOut}^0 \cdot \text{Req} \cdot \text{Wait}^1 \cdot \text{Ack} \cdot \text{Connected}^8$
- ▶ SEL : languages accepted by SE -automata without ε -transitions.
- ▶ SEL_ε : languages accepted by SE -automata with ε -transitions.

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3 Signal-Event (Timed) Substitutions

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Signal-Event (Timed) Substitutions

Definition

- ▶ Abstract alphabet : Σ_e and Σ_s
- ▶ Concrete alphabet : Σ'_e and Σ'_s
- ▶ Substitution σ from $SE(\Sigma)$ to $SE(\Sigma')$ defined by:

$$a \in \Sigma_e : L_a \subseteq (\Sigma'_e \cup \Sigma'_s \times \{0\})^*$$

$$\sigma(a) = L_a$$

$a \in \Sigma_s \setminus \{\tau\} : L_a \subseteq SE(\Sigma')$ **not containing Zeno words.**

$$\sigma(a^d) = \{w \in L_a \mid \|w\| = d\}$$

$$a = \tau : L_\tau = \{\tau\} \times \overline{\mathbb{T}}$$

$$\sigma(\tau^d) = \{\tau^d\}$$

Remark

If we allow Zeno words in L_a then we may get transfinite words as refinements.
Example: if $b^1 f b^{1/2} f b^{1/4} f \dots \in L_a$ and $L_g = \{g\}$ then $\sigma(a^2 g)$ is transfinite.

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Signal-Event (Timed) Substitutions

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In general, SE-substitutions are not morphisms

Example: if $L_a = \{b^2\}$ then $\sigma(a^1) = \emptyset$ and $\sigma(a^2) \neq \sigma(a^1)\sigma(a^1)$

Substitutions are applied to SE-words in **normal form**:

$$\sigma(a^2\tau^0a^1f\tau^0g\tau^1fb^2b^2b^2\cdots) = \sigma(a^3)\sigma(f)\sigma(g)\tau^1\sigma(f)\sigma(b^\infty)$$

Proposition

Let σ be a timed substitution, given by a family $(L_a)_{a \in \Sigma_e \cup \Sigma_s}$.

Then, σ is a morphism if and only if for each signal $a \in \Sigma_s$ we have

1. L_a is closed under concatenation:
for all $u, v \in L_a$ with $\|u\| < \infty$, we have $uv \in L_a$,
2. L_a is closed under decomposition:
for each $v \in L_a$ with $\|v\| = d$, for all $d_1 \in \mathbb{T}$, $d_2 \in \overline{\mathbb{T}}$ such that $d = d_1 + d_2$, there exist $v_i \in L_a$ with $\|v_i\| = d_i$ such that $v = v_1v_2$.

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Recognizable substitutions

Definition

Let σ be a substitution defined by $(L_a)_{a \in \Sigma_e \cup \Sigma_s}$. Then,

- ▶ σ is a *SEL* – substitution if each L_a is in *SEL*
- ▶ σ is a *SEL_ε* – substitution if each L_a is in *SEL_ε*

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Signal-Event (Timed) Substitutions

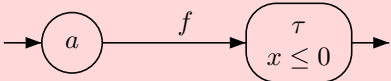
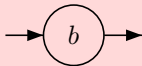
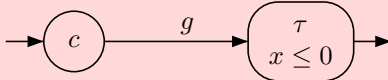
4 Closure under substitutions

Closure under inverse substitutions

Conclusion

Closure under substitutions

SEL is not closed under *SEL* – substitution

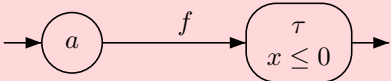
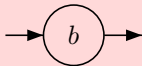
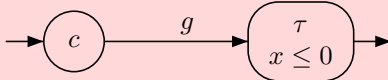
- ▶ $L = \{a^0 f\}$ is recognized by 
- ▶ $L_a = \{b\} \times \overline{\mathbb{T}}$ is recognized by 
- ▶ $L_f = \{c^0 g\}$ is recognized by 
- ▶ $\sigma(L) = \{b^0 c^0 g\}$ cannot be accepted without ε -transitions.

Theorem

1. The class SEL_ε is closed under SEL_ε -substitutions.
2. The class SEL is closed under SEL -substitution satisfying $L_f \subseteq \Sigma'_e((\Sigma'_s \times \{0\})\Sigma'_e)^*$ for each $f \in \Sigma_e$,
i.e., each word in L_f must start and end with an instantaneous event.

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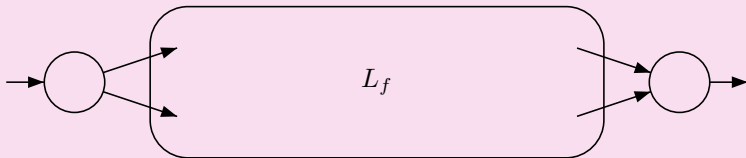
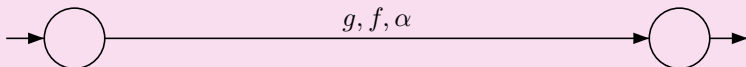
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Closure under substitutions

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Handling **events** is easy for SEL_ϵ -substitutions.

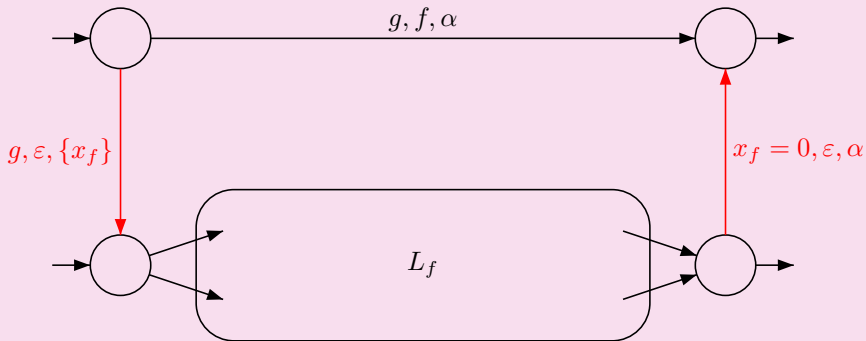


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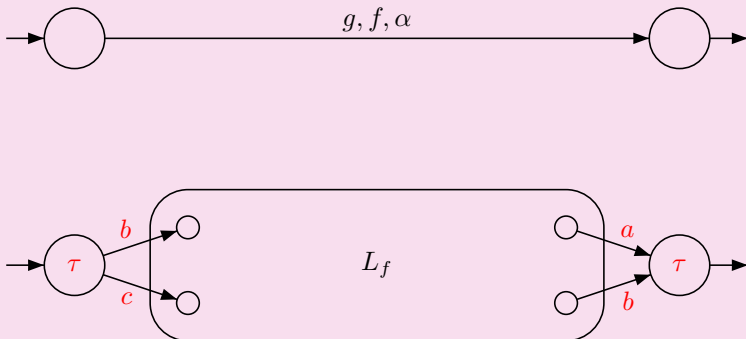


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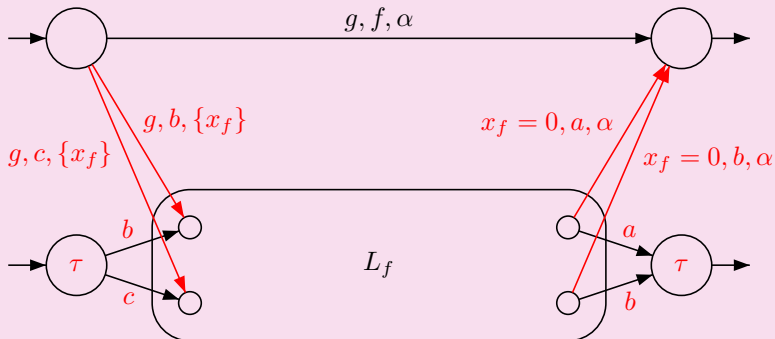


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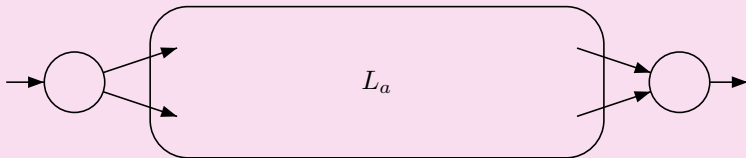
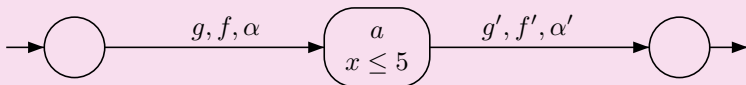


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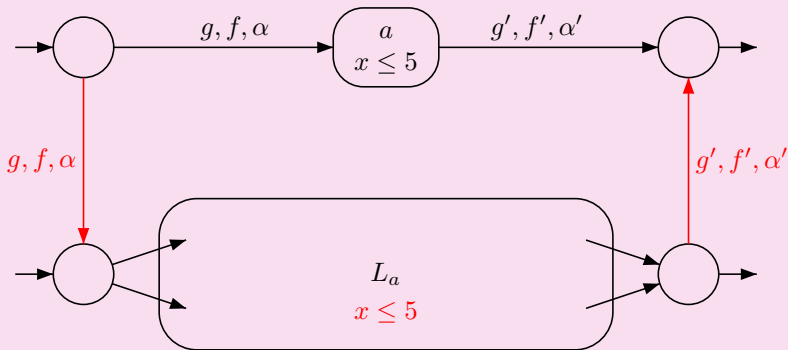


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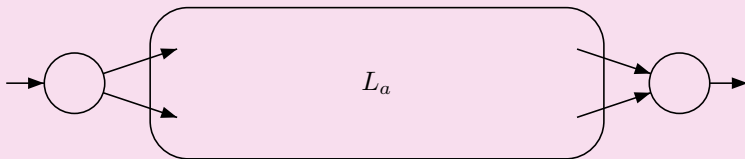
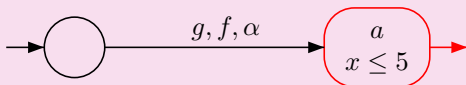


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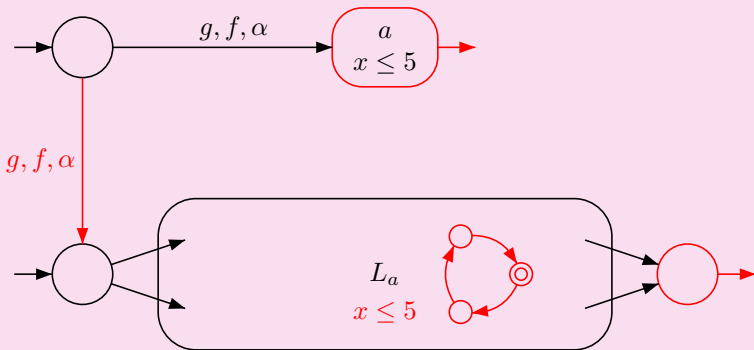


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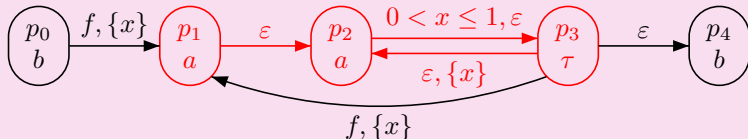
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Handling **signals** for SEL_ε -substitutions is **harder**.

Remember that substitutions are applied to SE-words in **normal form**.



A possible run gives : $f a^{0.3} a^{0.6} \tau^0 a^{0.5} \tau^1 a^{0.6} \tau^0 a^{0.5} \tau^0 b^3 \approx f a^{1.4} \tau^1 a^{1.1} b^3$

We have to synchronize a -blocks of \mathcal{A} with the automaton \mathcal{A}_a taking into account τ -states that may be crossed instantaneously.

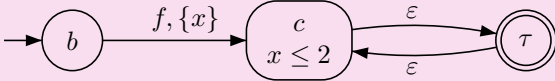
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Zeno runs in \mathcal{A}_a must be removed.

- ▶ L_a accepted by 
- ▶ $b^1 f c^2$ is accepted by an infinite Zeno run: $b^1 f c^1 \tau^0 c^{1/2} \tau^0 c^{1/4} \dots$
- ▶ We get $g b^1 f c^2 g \in \sigma(g a^3 g)$.

We have to replace the Zeno run of \mathcal{A}_a by a finite run.

Normal form for SE-automata

Theorem

Let \mathcal{A} be a SE-automaton. We can effectively construct an equivalent SE-automaton \mathcal{A}' such that:

1. no infinite run of \mathcal{A}' accepts a finite word with finite duration, and
2. no finite run of \mathcal{A}' accepts a word with infinite duration.

Main problem

We have to replace **infinite accepting ε -loops**

by **finite accepting runs**.

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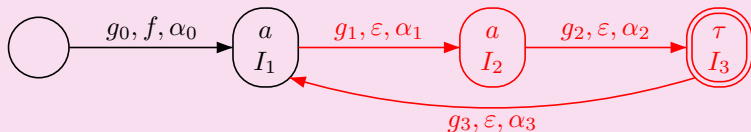
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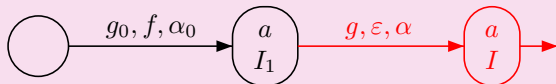
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Theorem

1. The class SEL_ε is closed under inverse SEL_ε -substitution.
2. The class SEL is closed under inverse SEL -substitution acting only on events:
 $L_a = \{a\} \times \overline{\mathbb{T}}$ for all $a \in \Sigma_s$.

The class SEL is not closed under arbitrary inverse SEL -substitution

- ▶ Let $\Sigma_s = \Sigma'_s = \{a, b\}$ and $\Sigma_e = \Sigma'_e = \{f\}$.
- ▶ Let σ be the SEL -substitution defined by $L_a = \{a^1 f\}$, $L_b = \{b^0\}$ and $L_f = \{f\}$.
- ▶ $L = \{a^1 f b^0\}$ is a SEL .
- ▶ $\sigma^{-1}(L) = \{a^1 b^0\}$ is not a SEL .

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1. The class SEL_ε is closed under inverse SEL_ε -substitution.
2. The class SEL is closed under inverse SEL -substitution acting only on events:
 $L_a = \{a\} \times \overline{\mathbb{T}}$ for all $a \in \Sigma_s$.

The class SEL is not closed under arbitrary inverse SEL -substitution

- ▶ Let $\Sigma_s = \Sigma'_s = \{a, b\}$ and $\Sigma_e = \Sigma'_e = \{f\}$.
- ▶ Let σ be the SEL -substitution defined by $L_a = \{a^1 f\}$, $L_b = \{b^0\}$ and $L_f = \{f\}$.
- ▶ $L = \{a^1 f b^0\}$ is a SEL .
- ▶ $\sigma^{-1}(L) = \{a^1 b^0\}$ is not a SEL .

Closure under inverse substitutions

Theorem

1. The class SEL_ε is closed under inverse SEL_ε -substitution.
2. The class SEL is closed under inverse SEL -substitution acting only on events:
 $L_a = \{a\} \times \overline{\mathbb{T}}$ for all $a \in \Sigma_s$.

Proof: word case

- ▶ Let $\sigma : A \rightarrow \mathcal{P}(B^*)$ be a rational substitution
- ▶ Let $\Pi_A : (A \uplus B)^* \rightarrow A^*$ and $\Pi_B : (A \uplus B)^* \rightarrow B^*$ be the projections
- ▶ Let $M = \left(\bigcup_{a \in A} a\sigma(a) \right)^* \subseteq (A \uplus B)^*$ is rational.
- ▶ Then, $\sigma^{-1}(L) = \Pi_A(\Pi_B^{-1}(L) \cap M)$

Closure under inverse substitutions

Theorem

1. The class SEL_ε is closed under inverse SEL_ε -substitution.
2. The class SEL is closed under inverse SEL -substitution acting only on events:
 $L_a = \{a\} \times \overline{\mathbb{T}}$ for all $a \in \Sigma_s$.

Proof: Signal-event words

- ▶ Let $\hat{\Sigma}_e = \Sigma_e \uplus \Sigma'_e$ and $\hat{\Sigma}_s = \Sigma_s \times \Sigma'_s$.
- ▶ Let $\Pi_1 : SE(\hat{\Sigma}) \rightarrow SE(\Sigma)$ and $\Pi_2 : SE(\hat{\Sigma}) \rightarrow SE(\Sigma')$ be the natural projections
- ▶ $\sigma^{-1}(L) = \Pi_1(\Pi_2^{-1}(L) \cap M)$ for a suitable language M , in the class SEL_ε .
if $f \in \Sigma_e$ then $f \cdot \sigma(f)$ is replaced by
 $f \cdot \{w \in SE(\hat{\Sigma}) \mid w = (\tau, b_0)^0 f_1(\tau, b_1)^0 f_2 \cdots (\tau, b_n)^0 \text{ with } b_0^0 f_1 b_1^0 f_2 \cdots b_n^0 \in \sigma(f)\}$
if $a \in \Sigma_s$ then $a \cdot \sigma(a)$ is replaced by
 $\{w \in SE(\hat{\Sigma}) \mid w = (a, b_0)^{d_0} f_1(a, b_1)^{d_1} f_2 \cdots \text{ with } b_0^{d_0} f_1 b_1^{d_1} f_2 \cdots \in \sigma(a^{d_0+d_1+\cdots})\}$
- ▶ If L is in the class SEL_ε , then so is $\Pi_2^{-1}(L)$.
- ▶ The class SEL_ε is closed under intersection.

Closure under intersection

Remark

- ▶ Easy for the class SEL or for classical timed languages.
- ▶ More difficult with signals and ε -transitions due to stuttering and unobservability of τ^0 .
- ▶ Asarin, Caspi and Maler 97 did not deal with these difficulties and considered finite runs only.
Asarin, Caspi and Maler 02 deals with the intersection of classical timed automata only.
- ▶ Dima 00 gives a construction to remove stuttering for automata with a single clock.
- ▶ Durand-Lose 04 gives a construction for intersection taking stuttering into account but restricted to finite runs and without zero-duration signals.
His approach do not extend to infinite runs since it would introduce Zeno runs leading to transfinite problems

Outline

Introduction

Signal-Event (Timed) Words and Automata

Signal-Event (Timed) Substitutions

Closure under substitutions

Closure under inverse substitutions

6 Conclusion

Conclusion

- ▶ Signal-event words are the natural objects for studying refinements, abstractions and other problems.
- ▶ Extending classical results to SE-automata is not always easy due to ε -transitions, signal stuttering, unobservability of τ^0 , Zeno runs, ...
- ▶ We have proved closure properties (intersection, refinement, abstraction) for the general case of SE-automata.