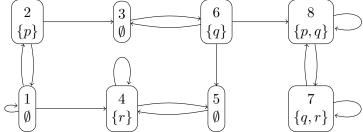
## Homework 3

To hand in on October 5th at 14:00, during the exercise session or by mail at marie.fortin@lsv.fr.

Exercise 1 (Semantics of CTL\*).



Compute the following sets for the given model:

- 1.  $\llbracket \mathsf{EG} \, r \rrbracket$
- 2.  $\llbracket \mathsf{AX} \, q \rrbracket$
- 3.  $\llbracket \varphi_1 \rrbracket$  where  $\varphi_1 = (\mathsf{EG}\, r) \vee (\neg q \wedge \mathsf{EX}\, q)$
- 4.  $\llbracket \mathsf{E} \psi \rrbracket$  where  $\psi = \mathsf{GF} \varphi_1 \to \mathsf{GF}(q \wedge \neg r)$

**Exercise 2** (Equivalences). Are the following formulæ equivalent? Give a proof or a counter example.

- 1.  $\mathsf{AXAG}\varphi$  and  $\mathsf{AXG}\varphi$
- 2.  $\mathsf{EXEG}\,\varphi$  and  $\mathsf{EXG}\,\varphi$
- 3.  $A(\varphi \wedge \psi)$  and  $A\varphi \wedge A\psi$
- 4.  $\mathsf{E}(\varphi \wedge \psi)$  and  $\mathsf{E} \varphi \wedge \mathsf{E} \psi$
- 5.  $\neg A(\varphi \Rightarrow \psi)$  and  $E(\varphi \land \neg \psi)$