

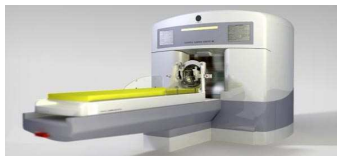
Verification of security protocols: from confidentiality to privacy

Stéphanie Delaune

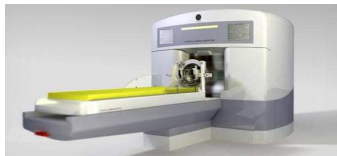
LSV, CNRS & ENS Cachan & INRIA Saclay Île-de-France, France

Friday, March 18th, 2011

Computers are everywhere!



Computers are everywhere!



A need for automated formal verification

- testing the system is not always sufficient
→ we want to consider **all** the possible behaviours
- manual proofs are tedious and error-prone
→ **automated** verification techniques



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Cryptographic protocols

- small programs designed to **secure** communication (*e.g.* secrecy)
- use **cryptographic primitives** (*e.g.* encryption, signature,)

The network is unsecure!

Communications take place over a **public** network like the Internet.

Cryptographic protocols



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Cryptographic protocols



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It becomes more and more important to protect our privacy.



Example: electronic passport

→ studied in [Arapinis *et al.*, 10]

An electronic passport is a passport with an **RFID tag** embedded in it.



The **RFID tag** stores:

- the information printed on your passport,
- a JPEG copy of your picture.

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The Basic Access Control (BAC) protocol is a key establishment protocol that has been designed to also ensure **unlinkability**.

ISO/IEC standard 15408

Unlinkability aims to ensure *that a user may make multiple uses of a service or resource without others being able to link these uses together.*

The electronic passport protocol

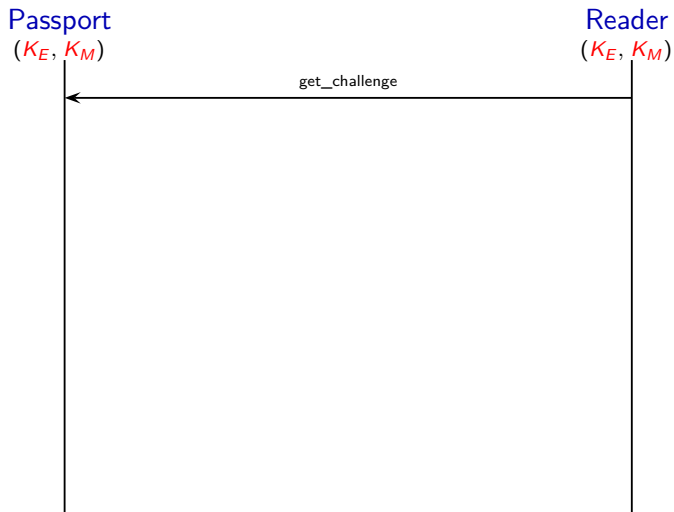
Passport
(K_E, K_M)



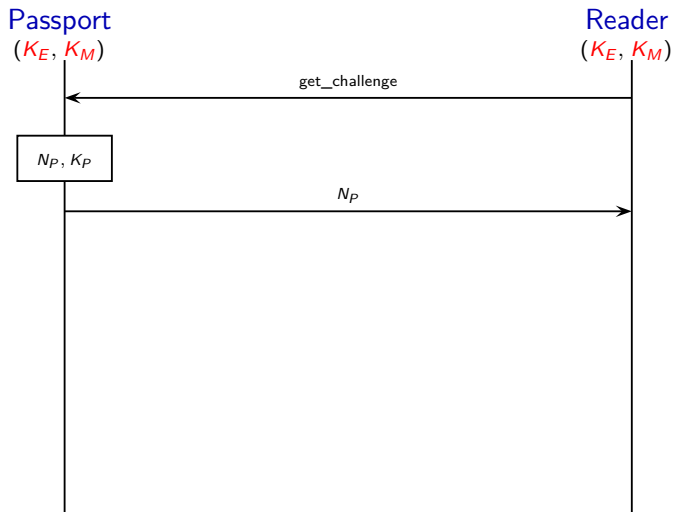
Reader
(K_E, K_M)



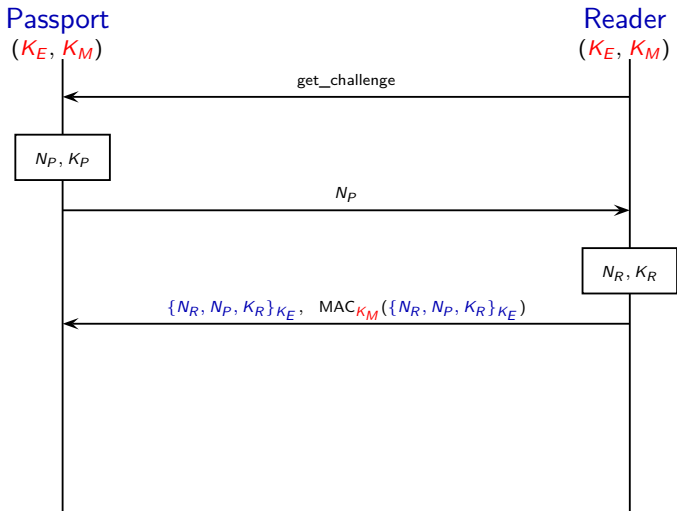
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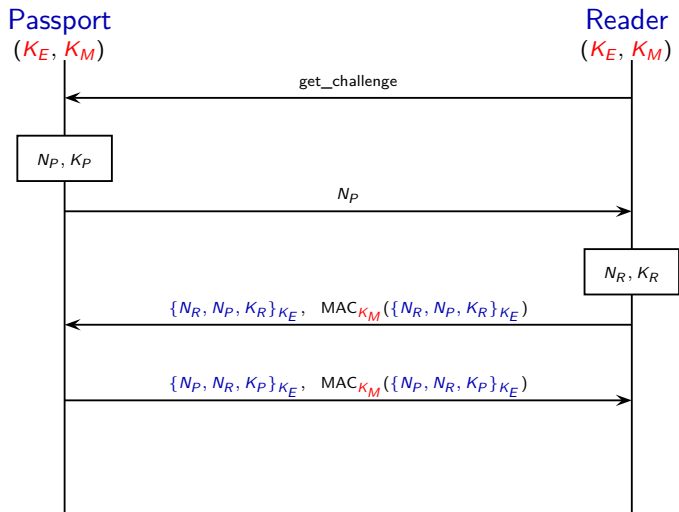
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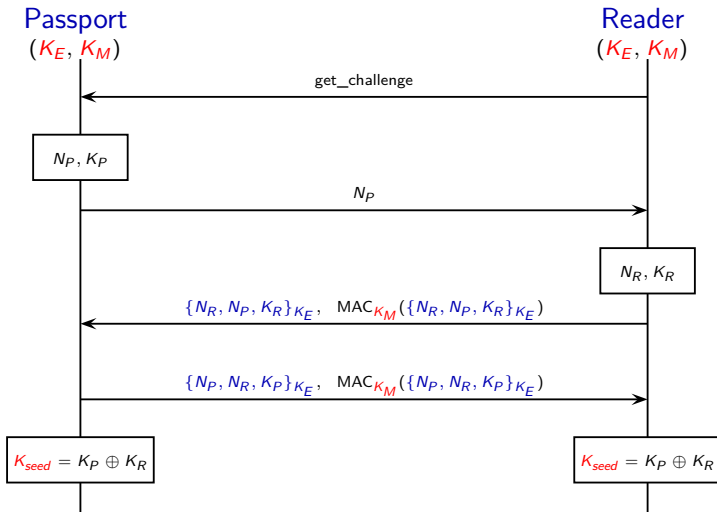
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Verification of cryptographic protocols (symbolic models)

→ Various models (e.g. [Dolev & Yao, 81]) having some common features

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Messages

They are abstracted by terms together with an equational theory.

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Examples:

→ symmetric encryption/decryption: $\text{dec}(\text{enc}(x, y), y) = x$

→ exclusive or operator:

$$\begin{aligned}(x \oplus y) \oplus z &= x \oplus (y \oplus z) & x \oplus x &= 0 \\ x \oplus y &= y \oplus x & x \oplus 0 &= x\end{aligned}$$

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Verification of cryptographic protocols (symbolic models)

→ **Various** models (e.g. [Dolev & Yao, 81]) having some **common** features



Messages

They are abstracted by **terms** together with an **equational theory**.

The attacker

- may **read** every message sent on the network,
- may **intercept** and **send** new messages according to its deduction capabilities.
→ only **symbolic** manipulations on terms.



State of the art in a nutshell

What about secrecy?

- several **undecidability** results for an **unbounded** number of sessions
[Even & Goldreich, 83; Durgin *et al*, 99]
- **decidability** results for a **bounded** number of sessions (NP-complete)
[Rusinowitch & Turuani, 01; Millen & Shmatikov, 01]
→ extended by many authors to deal with various primitives.

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Some automatic verification tools

- **AVISPA platform** [Armando *et al.*, 05]
→ state-of-the-art for bounded verification
- **ProVerif tool** [Blanchet, 01]
→ quite flexible to analyse security properties

→ None of the existing tools is able to analyse the e-passport protocol.

Formal analysis of new applications

Target applications: electronic voting protocols, RFID protocols, routing protocols, vehicular ad hoc networks, electronic auction protocols, ...

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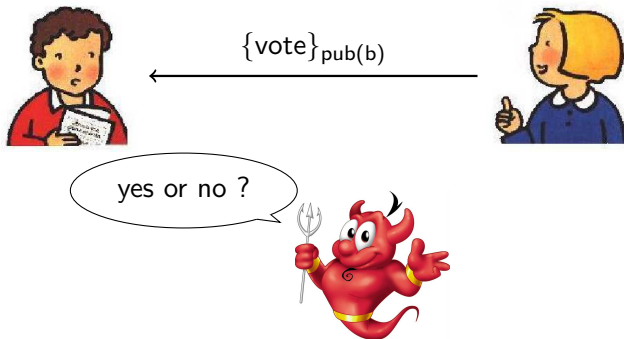
Challenges:

- 1 Formal definitions of the expected security properties
—→ **privacy-type** security properties
- 2 Designing appropriate **verification algorithms** that take into account the specific features of this new type of protocols
- 3 **Composition** results

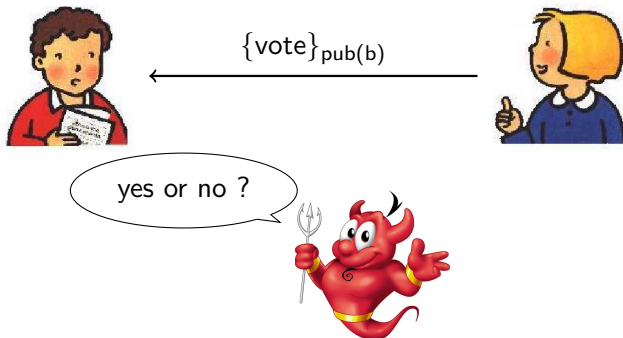
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A simple protocol



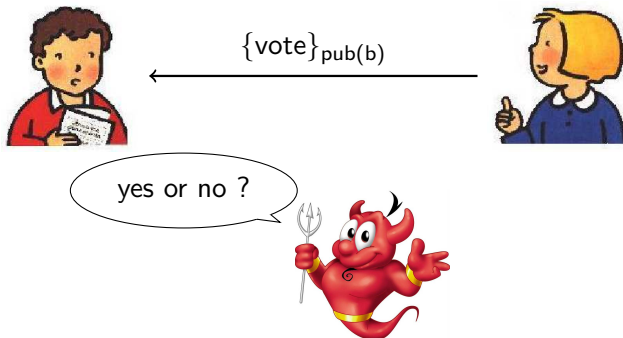
A simple protocol



Question

Does the attacker **know** Alice's vote?

A simple protocol



The real question

Is the attacker able to tell whether Alice sends **yes** or **no**?

Static equivalence (indistinguishability relation)

frame $\phi = \{M_1/x_1, \dots, M_\ell/x_\ell\}$

Static equivalence ($\phi \sim \phi'$)

[Abadi & Fournet, 01]

Two frames ϕ and ϕ' are **statically equivalent** if, and only if

$$C_1[M_1, \dots, M_\ell] = C_2[M_1, \dots, M_\ell] \Leftrightarrow C_1[M'_1, \dots, M'_\ell] = C_2[M'_1, \dots, M'_\ell]$$

for all **public** contexts C_1 , and C_2 .

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Example: ϕ_1 and ϕ_2 are **not** in static equivalence.

$$\phi_1 = \{\{\text{yes}\}_{\text{pub}(b)}/x\} \quad \text{and} \quad \phi_2 = \{\{\text{no}\}_{\text{pub}(b)}/x\}$$

$$\longrightarrow C_1 = \{\text{yes}\}_{\text{pub}(b)} \quad \text{and} \quad C_2 = x$$

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State of the art in 2006:

[Abadi & Cortier, 06]

- **PTIME** decision procedure for **subterm convergent equational theories**
→ e.g. **symmetric/asymmetric encryption, signature, ...**
- some abstract conditions that ensure **decidability** for many more theories
→ **exclusive or, homomorphic encryption, ...**

Some results for deduction and static equivalence (1/2)

A **generic procedure** implemented in the **YAPA tool** for deciding both notions for subterm convergent equational theories, blind signatures, homomorphic encryption, ...

<http://www.lsv.ens-cachan.fr/~baudet/yapa/index.html>

→ in collaboration with M. Baudet & V. Cortier

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Some equational theories motivated by the **e-voting application**
e.g. re-encryption, trapdoor bit commitment (**KiSs tool**), ...

<http://www.lsv.ens-cachan.fr/~ciobaca/kiss>

→ in collaboration with S. Ciobaca & S. Kremer

Some results for deduction and static equivalence (2/2)

Monoidal equational theories (AC operators)

e.g. exclusive or, abelian groups, ... together with some homomorphism laws

$$h(x + y) = h(x) + h(y)$$

General schema for deciding both problems:

- 1 **Reduce** both problems to classical algebraic problems.
- 2 Use existing results to conclude for **many** interesting equational theories.

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Combination results for disjoint theories

If deduction and static equivalence are decidable for E_1 and E_2 , then deduction and static equivalence are decidable for $E_1 \cup E_2$.

→ in collaboration with V. Cortier

Conclusion and perspectives

Conclusion

- Several **new** decidability and complexity results

Theory E	Deduction	Static equivalence
subterm convergent	PTIME	
blind signature	PTIME	
homomorphic encryption	decidable	
trapdoor commitment	PTIME	
ACUN	PTIME	PTIME
AG	PTIME	PTIME
ACUN _h /AG _h	PTIME	decidable
AG _h ₁ ... h _n	decidable	

Conclusion

- Several **new** decidability and complexity results ...
- that have been partly **implemented** (YAPA and KiSs).

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Some perspectives

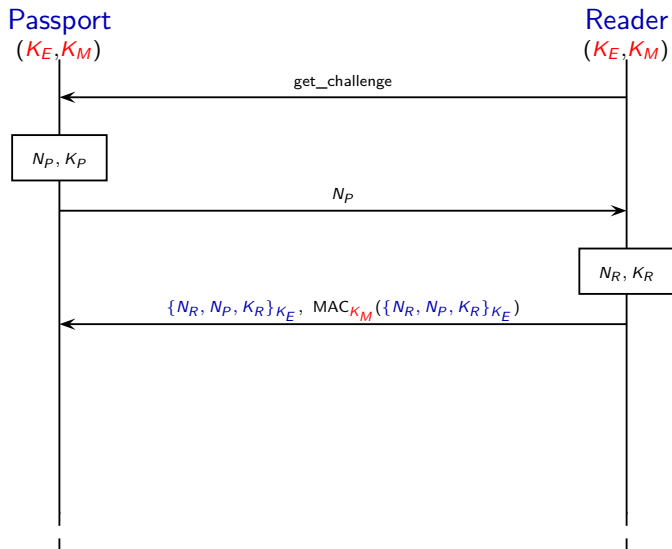
- **Extension** of YAPA and/or KiSs to theories with AC operators
- Combination for **non-disjoint** equational theories

More importantly, we have to move to the active case.

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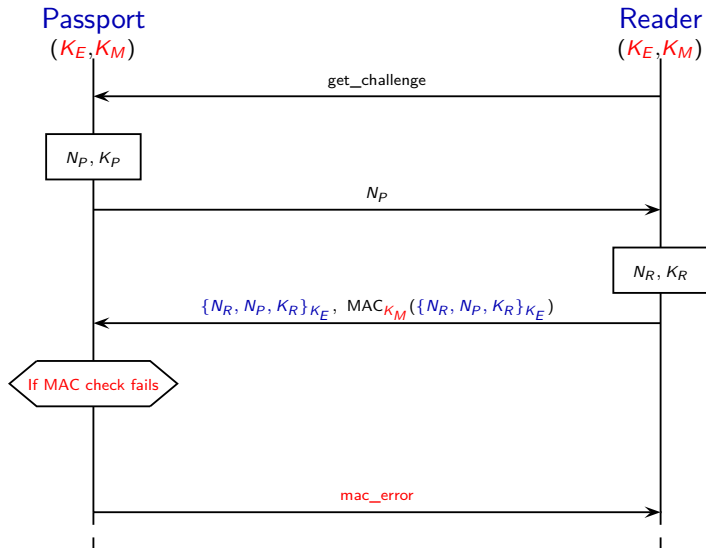
French electronic passport

→ the passport must reply to all received messages.



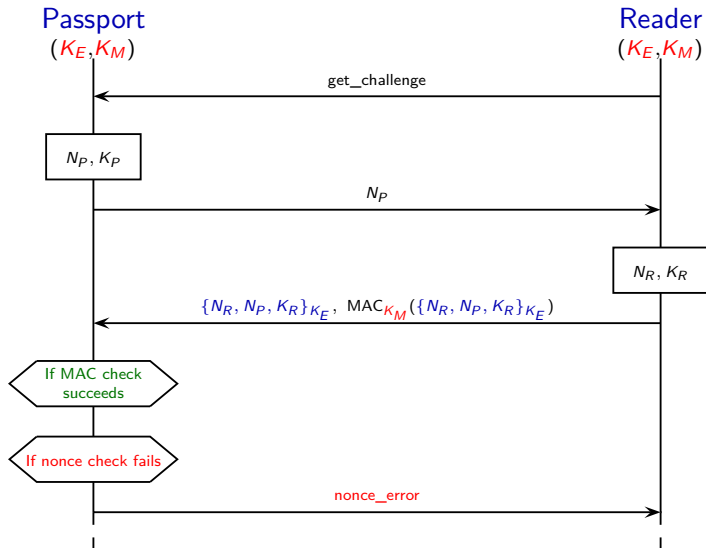
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Attack against unlinkability

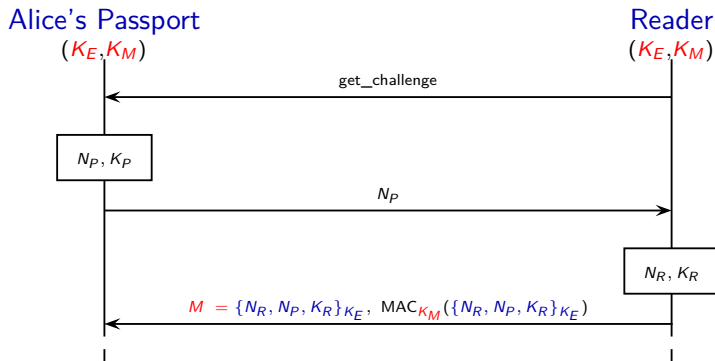
An attacker can track a French passport, provided he has once witnessed a successful authentication.

An attack on the French passport [Chothia & Smirnov, 10]

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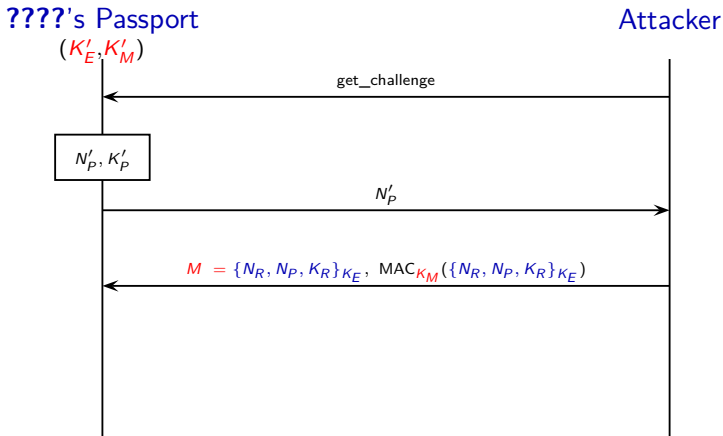
Part 1 of the attack. The attacker eavesdrops on Alice using her passport and records message M .



An attack on the French passport [Chothia & Smirnov, 10]

Part 2 of the attack.

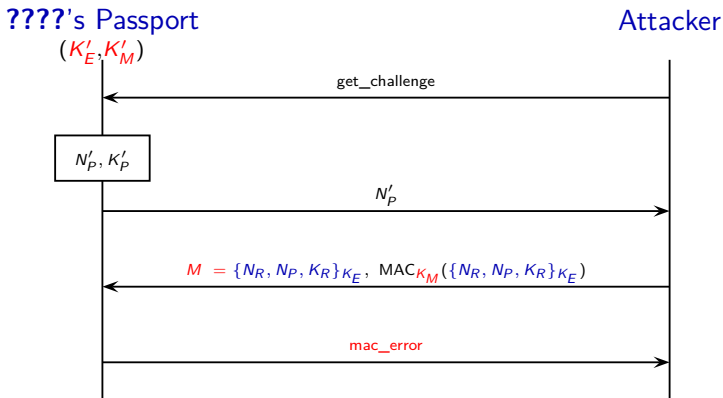
The attacker replays the message M and checks the error code he receives.



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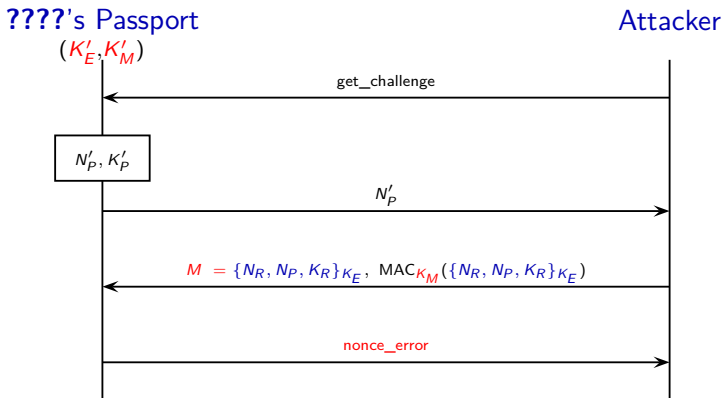


\implies MAC check failed $\implies K'_M \neq K_M \implies$ **????** is not Alice

An attack on the French passport [Chothia & Smirnov, 10]

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\implies MAC check succeeded $\implies K'_M = K_M \implies$??? is Alice

Some difficulties

Formalizing security properties and privacy-type properties is **rather subtle**.

- Privacy for electronic voting protocols
→ in collaboration with S. Kremer & M. Ryan
- Privacy in vehicular ad hoc network
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Observational equivalence

[Abadi & Fournet, 01]

The processes P and Q are **indistinguishable**, denoted $P \approx Q$, if for **all** attacker A we have that:

$$A \mid P \text{ can emit on } c \iff A \mid Q \text{ can emit on } c$$

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Automated protocol verifier mainly developed by **B. Blanchet**.

Main features

- **unbounded** number of sessions;
- **various** cryptographic primitives modeled using rewriting rules and equations;
- **various security properties**: (strong) secrecy, authentication, equivalence-based security properties.

The tool may not terminate or give false attacks. **It works well in practice.**

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Some results obtained with ProVerif

Formal analysis of **secrecy** and **authentication** properties in the TPM.



→ in collaboration with **S. Kremer, G. Steel, & M. Ryan**

Some limitations of the ProVerif tool

Observational equivalence

- ProVerif considers processes having the **same structure** (bi-process);
- the notion of equivalence, diff-equivalence, is **too strong**.

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Example

$$P = \text{out}(a) \mid \text{out}(b) \quad \text{and} \quad Q = \text{out}(b) \mid \text{out}(a)$$

We have that P and Q are **indistinguishable**, *i.e.* $P \approx Q$.

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Forming a bi-process, we obtain:

$$\text{out}(\text{choice}[a, b]) \mid \text{out}(\text{choice}[b, a]).$$

→ ProVerif is **not** able to conclude since they are **not** in diff-equivalence.

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We can also form the bi-process:

$$\text{out}(\text{choice}[a, a]) \mid \text{out}(\text{choice}[b, b]).$$

→ **ProVerif is able to conclude**. They are in diff-equivalence.

Contributions

We propose a **transformation** to **expand the scope** of ProVerif

Input: a bi-process P with some additional comment (** swap *)

Output: a bi-process Q on which ProVerif can directly reason, and
such that: P satisfies obs. equiv. $\Leftrightarrow Q$ satisfies obs. equiv.

→ in collaboration with B. Smyth & M. Ryan

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Recently, the transformation has been revisited [Smyth & Blanchet,10],
and implemented in the ProSwapper tool.

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Applications

- Electronic voting protocol by Fujioka, Okamoto, and Ohta (FOO)
- Direct Anonymous Attestation protocol based on the TPM (DAA)
→ in collaboration with B. Smyth & M. Ryan
- Vehicular ad hoc network (CMIX protocol, E-toll collection protocol)
→ in collaboration with M. Dahl & G. Steel

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Secrecy problem via constraint solving

→ for a fixed number of sessions

Protocol rules

in(u_1); out(v_1)

in(u_2); out(v_2)

...

in(u_n); out(v_n)

Constraint system

$$\mathcal{C} = \left\{ \begin{array}{l} T_0 \stackrel{?}{\vdash} u_1 \\ T_0, v_1 \stackrel{?}{\vdash} u_2 \\ \dots \\ T_0, v_1, \dots, v_n \stackrel{?}{\vdash} s \end{array} \right.$$

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Solution of a constraint system \mathcal{C}

A substitution σ such that

for every $T \stackrel{?}{\vdash} u \in \mathcal{C}$, we have that $u\sigma$ is deducible from $T\sigma$.

Main idea of the decision procedure

There exist some algorithms (actually a set of simplification rules) to decide whether such kind of constraint systems have a solution or not.

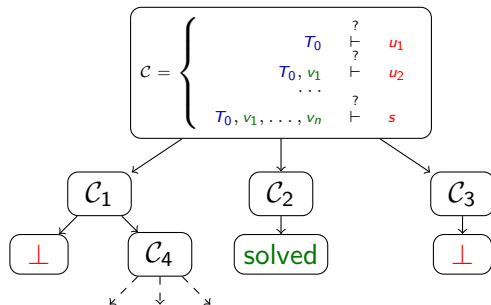
[Millen & Shmatikov, 01; Comon *et al.*, 09]

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Main idea of the procedure:



→ this gives us a symbolic **representation** of **all** the solutions.

Some results

We extend this procedure to other kind of constraints

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Other cryptographic primitives

- a generic result for **good** inference systems that are **finite**;
- blind signatures (used in e-voting): $v \stackrel{?}{\in} Bd(T, u)$,

$$\frac{\text{sign}(\text{blind}(x, y), z) \quad y}{\text{sign}(x, z)}$$

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Routing protocols

- **Disequality** constraints of the form $\forall X. v \neq u$.
- **Neighborhood** constraints: e.g. $\text{check}(a, b)$

→ Part of PhD work of M. Arnaud

Step 1: From observational equivalence to symbolic equivalence

→ reduce the problem of deciding an equivalence-based properties on processes to a decision problem on constraint systems.

- ① **general processes** expressed in the applied pi calculus
→ in collaboration with S. Kremer & M. Ryan
- ② **simple processes**
→ in collaboration with V. Cortier

Equivalence-based security properties via constraint solving

Step 1: From observational equivalence to symbolic equivalence

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Step 2: Decision procedure for symbolic equivalence

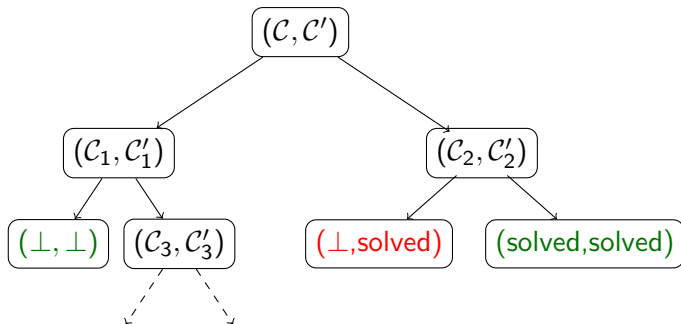
→ several procedures already exist,

e.g. [Baudet, 05; Chevalier & Rusinowitch, 09].

- 1 a **new procedure** based on a set of simplification rules
- 2 **implementation**: the ADECS tool
<http://www.lsv.ens-cachan.fr/~cheval/program/adecs/>
→ part of PhD work of V. Cheval

Our procedure in a nutshell

Main idea: We rewrite pairs of constraint systems (extended to keep track of some information) until a trivial failure or a trivial success is found.



Some perspectives

How can we expand further the scope of ProVerif?

→ more cryptographic primitives (*e.g.* exclusive or)

- by relying on the **finite variant property** as done in [Küsters & Truderung, 10] for trace-based security properties;
- **Application**: RFID protocols.

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- **Application**: RFID protocols.

Constraint solving approach

- Algorithms for symbolic equivalence for **more general** systems
e.g. disequality tests, more primitives
- Moving from symbolic equivalence of **pairs** of constraints to symbolic equivalence of **sets** of constraints
→ *This will allow us to analyse the e-passport protocol*
- **Efficient procedure** to reduce equivalence of processes to symbolic equivalence of constraints

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- 1 Formal definitions of the expected security properties
→ **privacy-type** security properties
- 2 Designing appropriate **verification algorithms** that take into account the specific features of this new type of protocols
- 3 **Composition** results

Security issues in mobile ad hoc network

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- security properties: privacy, route validity
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Verification issues

- we need to extend the verification techniques to integrate these new features
- **reduction results** to simplify the topology, the attacker model, . . .

Privacy-type properties

A taxonomy for privacy-type properties

For many applications (*e.g.* routing protocols), formal definitions of privacy-type properties are **still missing**.

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Verification algorithms (in the active setting)

First step: an **efficient verification tool** (for a bounded number of sessions) allowing us to deal with:

- e-passport protocol - see [Arapinis *et al.*, 10]
- private authentication protocols - see [Abadi & Fournet, 04]

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Second step:

- **more primitives:** subterm convergent, monoidal, and combination results
- integrate some **specific features** depending on the target applications

Motivations

- Existing tools allow us to verify **relatively small** protocols and sometimes only for a **bounded number of sessions**
- Most often, we verify them in **isolation**

Protocols do not compose well as soon as they share data.

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$$P_2 : A \rightarrow B : \{N_a\}_{\text{pub}(B)}$$
$$B \rightarrow A : N_a$$

Question: What about the secrecy of s ?

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Main goal: Investigate **sufficient conditions** under which protocols can be safely composed.

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Main goal: Investigate **sufficient conditions** under which protocols can be safely composed.

- From one protocol to many (secrecy, authentication, password-based protocols)
→ in collaboration with V. Cortier, S. Kremer, & M. Ryan
- From one sessions to many
→ in collaboration with M. Arapinis & S. Kremer

Composition

- What about protocols that involve an arbitrary number of agents?
- What about equivalence-based properties?

→ establish unlinkability for **two tags** and obtain guarantee in a setting that involves **an arbitrary number of tags**.

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Symbolic Universal Composability (UC)

A paradigm that has been quite successful in the computational approach.

$$\exists \mathcal{S} \text{ such that } \mathcal{F} \approx \mathcal{S}[P]$$

→ in collaboration with S. Kremer & O. Pereira

- bring the benefit of this approach in the symbolic setting;
- analysis of **more sophisticated protocols** specified by an ideal functionality.

The results presented in this habilitation thesis have been obtained in collaboration with many other researchers that are listed below:

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